

International Spring School Statistical Thermodynamics, Santiago de Chile  
Tuesday, November 28, 2017  
Lecture 17

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# On comparing simulated with experimental data

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# On comparing molecular modelling results with experimental data

## A. The experimental problem

1. Experimental data  $Q^{\text{exp}}$  are averaged
2. Insufficient number of experiments
3. Insufficient accuracy of experimental data
4. Experimental data  $Q^{\text{exp}}$  may be inconsistent

## B. Six aspects

1. Measured (primary) versus derived (secondary) data
2. How to handle averaging
3. Sensitivity of  $\langle Q \rangle_{\text{sim}}$  or  $\langle Q \rangle_{\text{exp}}$  to the conformational distribution
4. Compensation of (simulation/experimental) errors
5. Biasing of the simulation towards experiment
6. Identity of calculated versus measured quantities or systems

## C. Interpretation of experimental data using simulation

1. Relation between average  $\langle Q \rangle$  and conformational distribution  $P(r)$
2. Four reasons for agreement between  $\langle Q \rangle_{\text{sim}}$  and  $\langle Q \rangle_{\text{exp}}$
3. Five reasons for disagreement between  $\langle Q \rangle_{\text{sim}}$  and  $\langle Q \rangle_{\text{exp}}$

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# Comparison with Experimental Data for a Quantity Q

$$\langle Q \rangle_{sim} \leftrightarrow \langle Q \rangle_{exp}$$

W.F. van Gunsteren, J. Dolenc, &  
A.E. Mark, *Curr. Opin. Struct. Biol.*,  
18 (2008) 149-153

Distinguish between:

1. **primary** experimental data  $Q^{measured}$ : *observable* quantities Q that are **directly measured**

Examples: peak location and intensity from X-ray diffraction or NMR spectroscopic measurements (a.o.  $^3J$ -values)

2. **secondary** (*derived using a model*) "experimental" data  $Q^{derived}$ : quantities Q for which (*non-observed*) values are **derived from** (observed) values of primary experimental data  $Q^{measured}$  by applying a particular **procedure f**:  $Q^{derived} = f(Q^{measured})$  which involves assumptions and approximations

Examples: *molecular structures* (a.o. torsional angle values)  
NMR order parameters

Comparison of

a.  $\langle Q^{measured} \rangle_{sim}$  with  $\langle Q^{measured} \rangle_{exp}$

b.  $\langle Q^{derived} \rangle_{sim}$  with  $\langle Q^{derived} \rangle_{exp} = f(\langle Q^{measured} \rangle_{exp})$

may reflect the quality of:

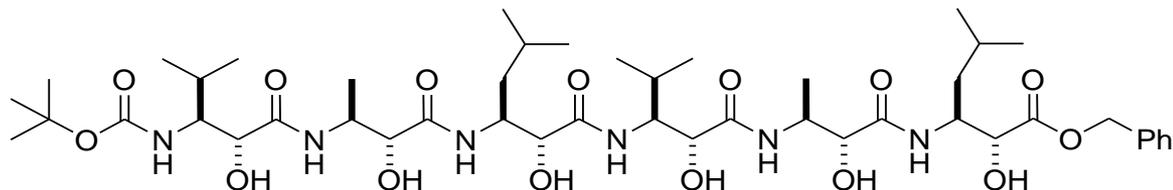
the **simulation**

the **procedure f**

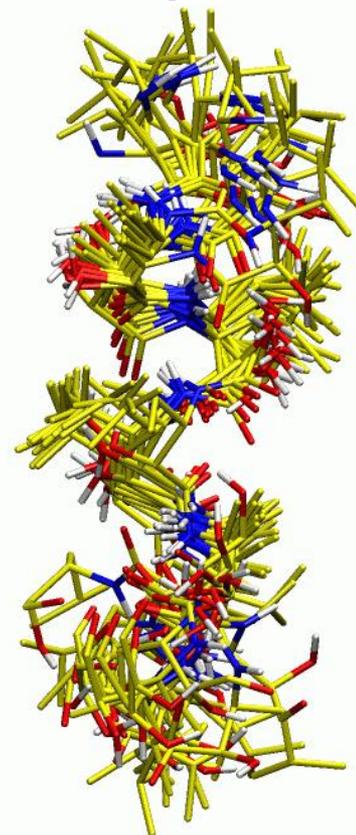
**In reality  $\langle Q^{derived} \rangle_{exp}$  may carry little experimental information**

# A $\beta$ -hexapeptide

Two non-overlapping conformational ensembles reproduce the experimental data:  
Which one is realistic?



- $\beta$ -hexapeptide with hydroxyl groups attached to the  $\alpha$ -carbons
- NMR single-structure refinement *based on NOE and  $^3J$ -coupling data* suggests the formation of a  $2_8$ -**P**-helix
- MD simulation from totally extended conformation at two different temperatures (298 K & 340K) using the GROMOS 45A3 force field *without any NOE-distance or  $^3J$ -value restraining* suggests the formation of a  $2.5_{12}$ -**P**-helix



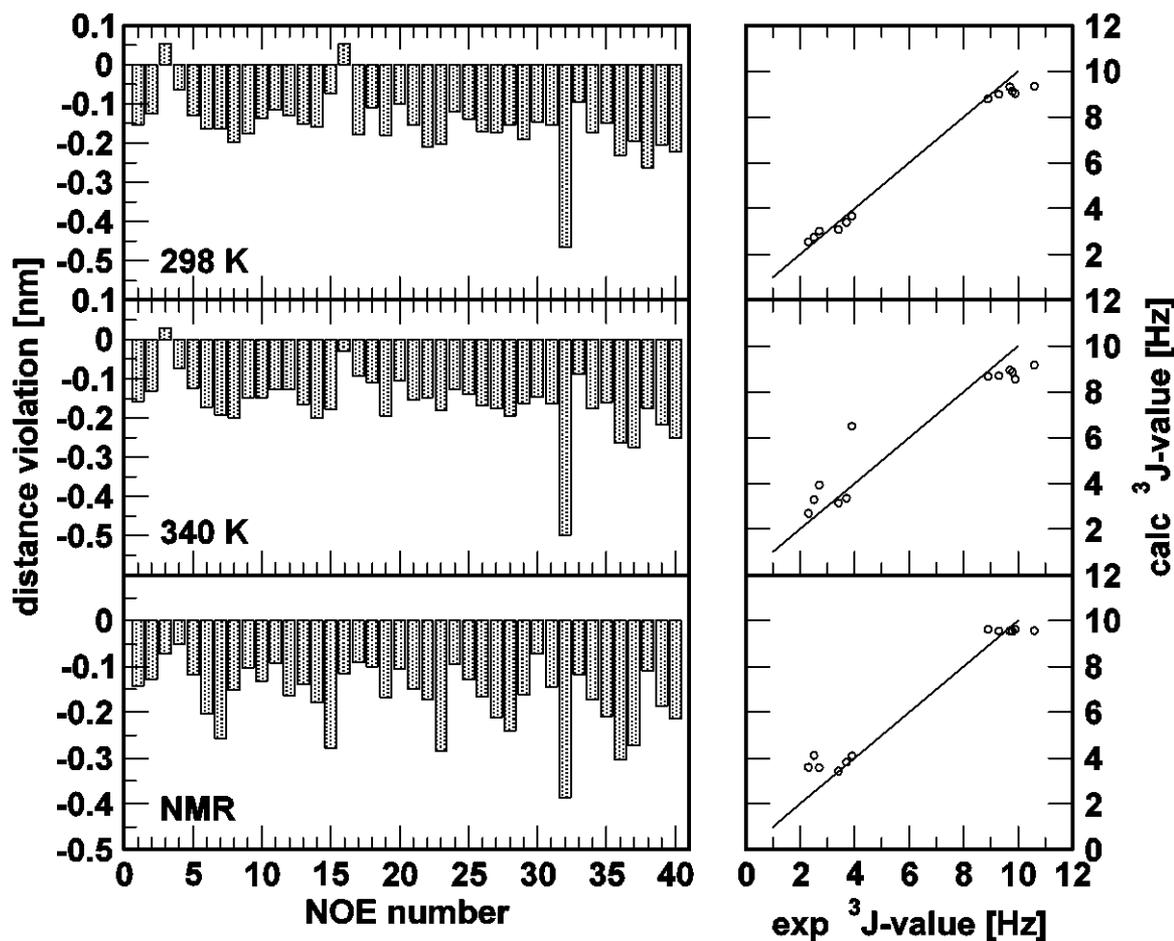
Bundle of 20 NMR model structures

(protection groups not shown)

Gademann et al., *Angew. Chem. Int. Ed. Engl.* 42 (2003) 1534

Glaettli & van Gunsteren, *Angew. Chem. Int. Ed. Engl.* 43 (2004) 6312

# NOE Distance Violations & Backbone $^3J$ -values



- MD at 298 K  
2 violations ( $\sim 0.05$  nm)  
average deviation from  
exp. J-values: 0.44 Hz
- MD at 340 K  
1 violation ( $\sim 0.03$  nm)  
average deviation from  
exp. J-values: 0.91 Hz
- NMR set of structures  
no violation (0.0 nm)  
average deviation from  
exp. J-values: 0.57 Hz

Two different methods to derive a set of peptide structures produce **non-overlapping ensembles** that each **reproduce the measured data**. However **MD simulation (ensemble)** predicts a well known  **$2.5_{12}$ -helix**, whereas the **NMR single-structure refinement** predicts an **unknown  $2_8$ -helix**

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# The Molecular Modelling Approach

How to calculate a quantity or observable  $Q(\vec{r})$  ?

## Choose:

1. (essential) degrees of freedom  $\vec{r}$   
↳ for  $Q(\vec{r})$     **electronic**  
                          **atomic**  
                          **solvent**
2. interaction function  $V^{phys}(\vec{r})$   
    between degrees of freedom (force field, e.g. GROMOS)
3. equations of motion or sampling method  
    to generate a Boltzmann-weighted ensemble of conformers:  
    probability  $P(\vec{r}) = \exp(-V^{phys}(\vec{r})/k_B T) / \int \exp(-V^{phys}(\vec{r})/k_B T) d\vec{r}$
4. function  $Q(\vec{r})$  (contains approximations and assumptions)

Ensemble averages

$$\langle Q \rangle_{\vec{r}} \equiv \int Q(\vec{r}) P(\vec{r}) d\vec{r}$$

are to be compared:

$$\langle Q \rangle_{sim}$$

**is to be compared to**

$$\langle Q \rangle_{exp} \equiv Q^{exp}$$

## If

1.  $V^{phys}(\vec{r})$  and  $Q(\vec{r})$  **are correct**
  2. **infinite** sampling
- } **problem solved**

## Otherwise

make other choices and repeat

# Effects of Ensemble (Motional) Averaging

$$\langle Q(\vec{r}) \rangle_{\vec{r}} \equiv \int Q(\vec{r}) P(\vec{r}) d\vec{r} \equiv \frac{\int Q(r) e^{-V^{phys}(\vec{r})/k_B T} d\vec{r}}{\int e^{-V^{phys}(\vec{r})/k_B T} d\vec{r}}$$

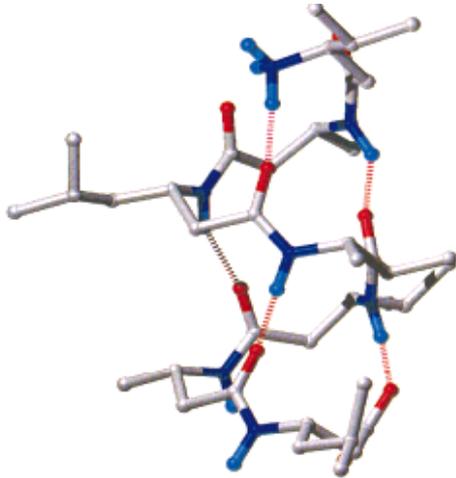
$\langle Q(\vec{r}) \rangle_{\vec{r}}$ averaged $Q$	$\neq$	$Q(\vec{r})$ single structure $Q$
$\neq$	$\neq$	$Q(\langle \vec{r} \rangle_{\vec{r}})$ mean structure $Q$

Examples of (*observable*) quantities  $Q(r)$ : *Boltzmann weighting is non-linear*  
*Function  $Q(r)$  may be non-linear*

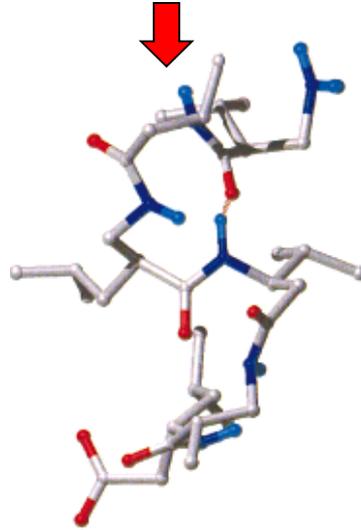
- NOE intensities (NMR)
- $^3J$ -coupling constants (NMR)
- Residual dipolar couplings (NMR)
- Chemical shifts (NMR)
- Structure factors (amplitudes) (X-ray)
- CD spectra (CD)
- .....

# Effect of Ensemble (Motional) Averaging

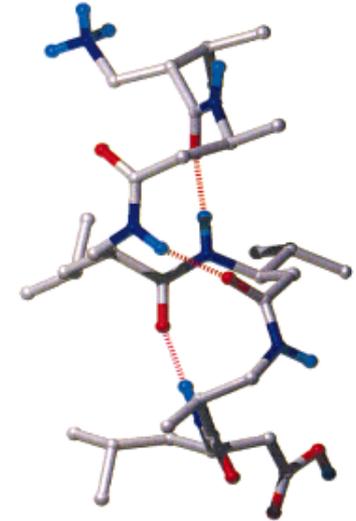
The **average structure**  $\langle r \rangle_r$  is highly strained for a 6- $\beta$ -peptide in methanol: 34 NOE's



**left-handed  $3_{14}$ -helix**  
of a similar peptide in MeOH  
H-bonds: NH(i) – O(i+2)



**average structure:**  
**distorted right-handed helix in MeOH only one**  
H-bond: NH(4) – O(1)



**right-handed helix in pyridine**  
H-bonds: NH(i) – O(i+1, i-3)

due to 3 NOE's characteristic → not observed in pyridine  
for a left-handed  $3_{14}$ -helix

**MD simulation:** - satisfies all NOE bounds  
- shows 35% *right-handed* helix  
1.3% *left-handed* helix

**Conclusion:** - average structure may be meaningless  
- use **primary (observed)** exp. data (NOE's),  
**not secondary (derived)** exp. data (structures) **to compare with**

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## Relation between average $\langle Q \rangle$ and conformational distribution $P(\vec{r})$

When relating the *average* of a property over a given conformational distribution  $P(\mathbf{r})$ , whether from a simulation ( $\langle Q \rangle_{sim}$ ) or measured experimentally ( $\langle Q \rangle_{exp}$ ), to the conformational distribution itself, **three general cases** can be distinguished:

- Q1**  $\langle Q \rangle$  does not reflect the shape of  $P(\mathbf{r})$  as  $\langle Q \rangle$  is **insensitive** to conformation
- Q2**  $\langle Q \rangle$  does not reflect the shape of  $P(\mathbf{r})$  as  $\langle Q \rangle$  is determined by **rarely sampled** conformations with small (*irrelevant*) Boltzmann weights
- Q3**  $\langle Q \rangle$  **does reflect** the dominant conformations of  $P(\mathbf{r})$

Only in case **Q3** can  $\langle Q \rangle_{sim}$  carry information relevant to the interpretation of  $\langle Q \rangle_{exp}$  at a molecular level

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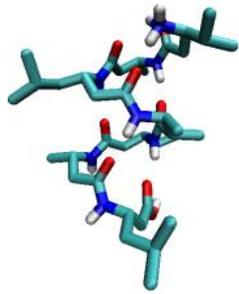
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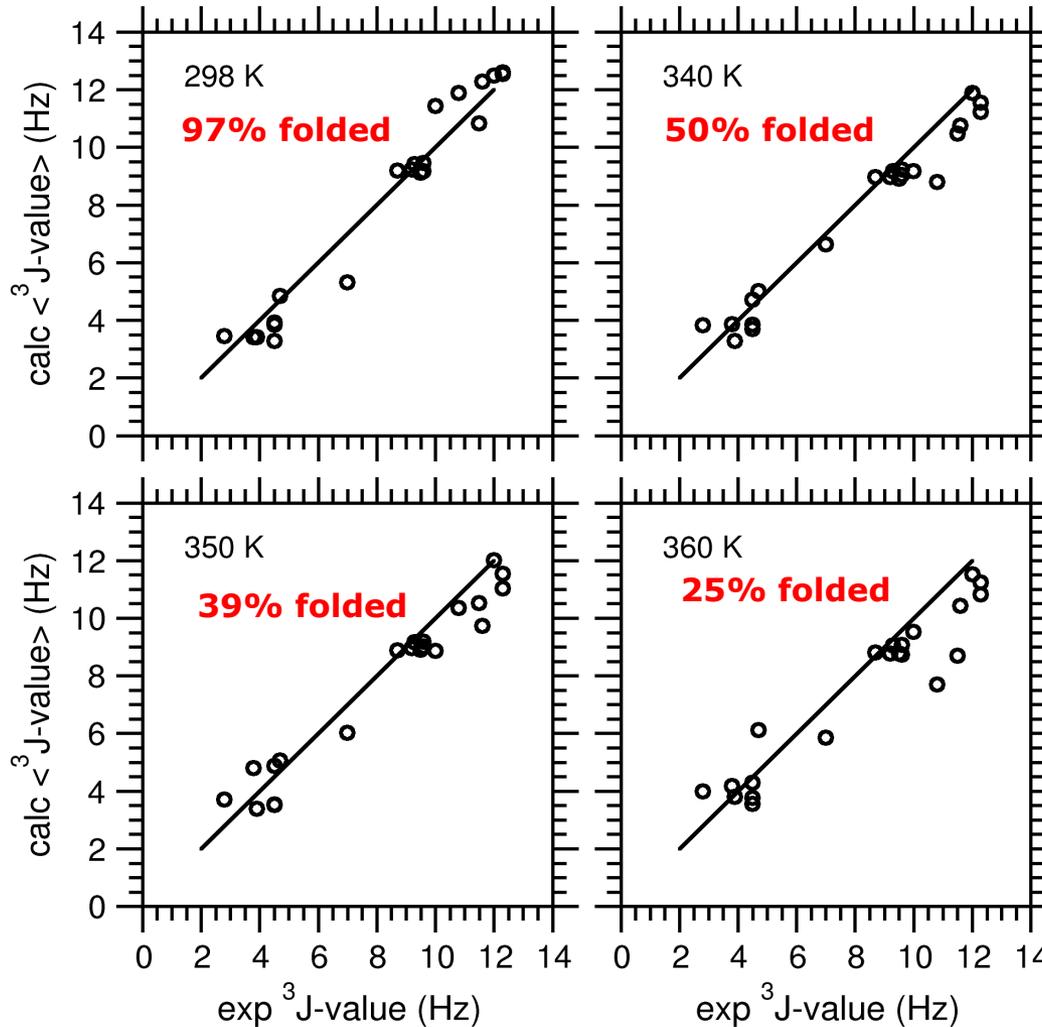
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# Different Ensembles of a 7- $\beta$ -peptide in solution



**3<sub>14</sub>-L-helix**



$^3J(\text{H}_N\text{-H}_{\alpha \text{ or } \beta})$ -couplings are *insensitive* to the conformational distribution

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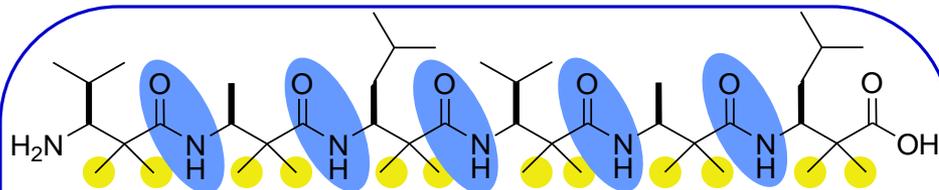
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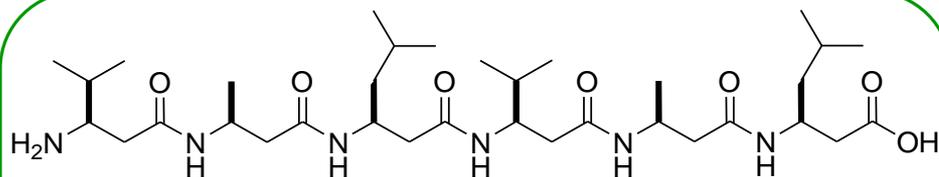
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# Calculation of Circular Dichroism (CD) Spectra



## Peptide A: DM-BHP (methyls (yellow))

- geminal dimethylation inhibits the formation of a  $3_{14}$  helix
- no NMR data available
- CD spectrum shows a pattern, which is “typical” for a  $3_{14}$  helix



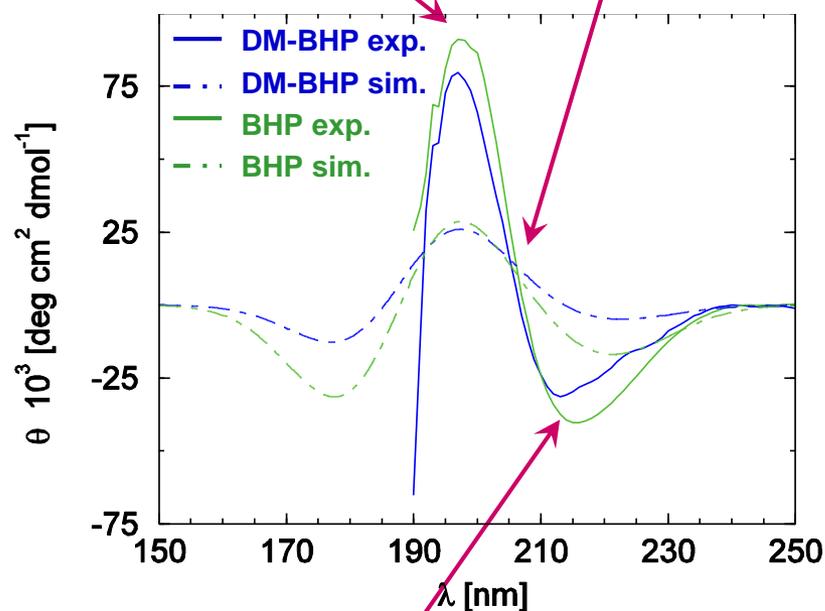
## Peptide B: BHP (no methyls)

- can adopt a  $3_{14}$  helix, confirmed by NMR experiments, CD spectrum similar

Two molecules with *similar* CD spectra, but cannot have a *similar* dominant structure

positive Cotton effect at  $\sim 200$  nm

zero crossing between 205 and 210 nm

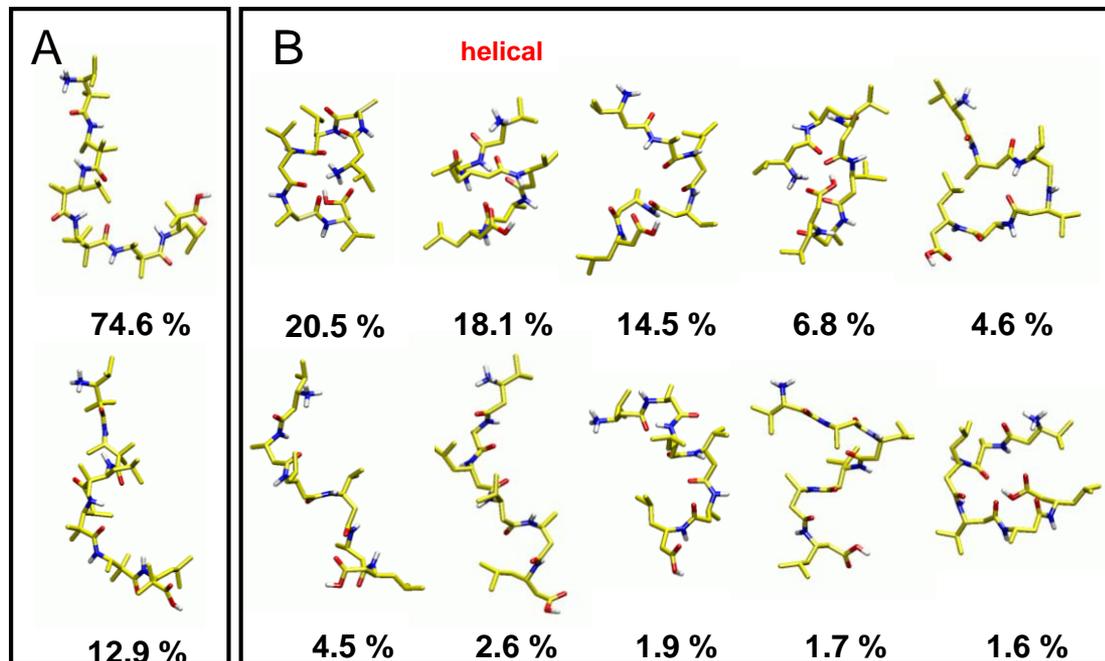
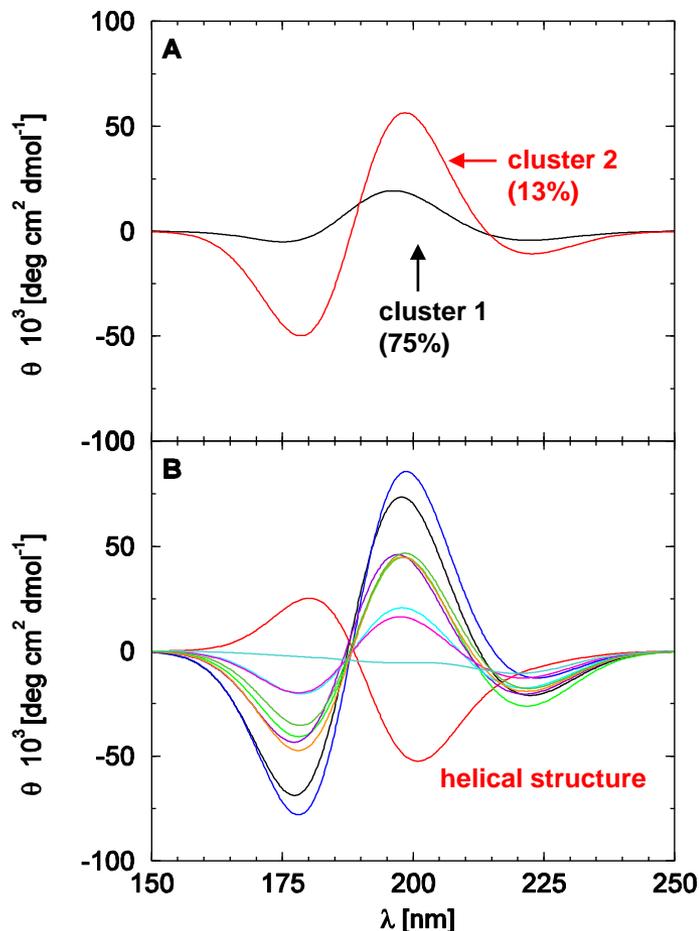


negative Cotton effect between 215 and 220 nm

# CD Spectra per Conformational Cluster

Similarity criterion: backbone RMSD  $\leq 0.09\text{nm}$

10000 structures, 10 psec apart



Non-helical conformers exhibit the CD pattern assigned to the  $3_{14}$  helix, the "helical" conformer doesn't.

→ virtually NO OVERLAP between the conformational ensembles of both molecules, which have similar CD spectra !

→ spectrum *not representative* for the dominant conformation !

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Reasons for **agreement** between  $\langle Q \rangle_{sim}$  and  $\langle Q \rangle_{exp}$

Agreement between  $\langle Q \rangle_{sim}$  and  $\langle Q \rangle_{exp}$  may be obtained if:

- A1**  $\langle Q \rangle$  is **insensitive** to  $P(\mathbf{r})$ , i.e.  $\langle Q \rangle_{sim}$  matches  $\langle Q \rangle_{exp}$  irrespective of the conformational distribution  $P(\mathbf{r})$  simulated
- A2** There are **compensating errors** in the simulation model, procedure or experimental set-up
- A3** The experimental data of interest,  $\langle Q \rangle_{exp}$ , has been used to **bias** the simulation
- A4**  $\langle Q(\mathbf{r}) \rangle_{sim}$  is **sensitive** to the distribution  $P(\mathbf{r})$

Only in the case **A4** can the degree of agreement between  $\langle Q \rangle_{sim}$  and  $\langle Q \rangle_{exp}$  be used to validate the simulation and/or to interpret the experimental results

# Interpretation of Experimental Data using Simulation

Reasons for agreement between  $\langle Q \rangle_{sim}$  and  $\langle Q \rangle_{exp}$

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# On comparing molecular modelling results with experimental data

## A. The experimental problem

1. Experimental data  $Q^{\text{exp}}$  are averages over time and space
2. Insufficient number of experimental data  $Q^{\text{exp}}$
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## B. Six aspects

1. *Measured* (primary) versus *derived* (secondary) data
2. How to handle averaging
3. Sensitivity of  $\langle Q \rangle_{\text{sim}}$  or  $\langle Q \rangle_{\text{exp}}$  to the conformational distribution  $P(r)$
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5. Biasing of the simulation towards experiment
6. Identity of calculated versus measured quantities or systems

## C. Interpretation of experimental data using simulation

1. Relation between average  $\langle Q \rangle$  and conformational distribution  $P(r)$
2. Four reasons for agreement between  $\langle Q \rangle_{\text{sim}}$  and  $\langle Q \rangle_{\text{exp}}$
3. Five reasons for *disagreement* between  $\langle Q \rangle_{\text{sim}}$  and  $\langle Q \rangle_{\text{exp}}$

# Interpretation of Experimental Data using Simulation

Reasons for **disagreement** between  $\langle Q \rangle_{sim}$  and  $\langle Q \rangle_{exp}$

Failure to observe a correlation between the simulation and experiment can be due to many reasons:

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- a) relevant degrees of freedom were omitted;
- b) the force field was insufficiently accurate;
- c) approximations made when solving the equations of motion were too crude;
- d) inappropriate thermodynamic or spatial boundary conditions were used.

**D2** The **measured**  $\langle Q \rangle_{exp}$  is **inaccurate**

**D3**  $\langle Q \rangle_{sim}$  and  $\langle Q \rangle_{exp}$  are **averaged differently** with respect to time or spatial extent

**D4** Related but **different quantities** are compared, e.g. atom-positional fluctuations versus crystallographic B factors

**D5** **Different systems** are compared (e.g. crystal versus solution), or systems studied under different thermodynamic conditions (e.g. temperature, pressure, pH, ionic strength, etc.)

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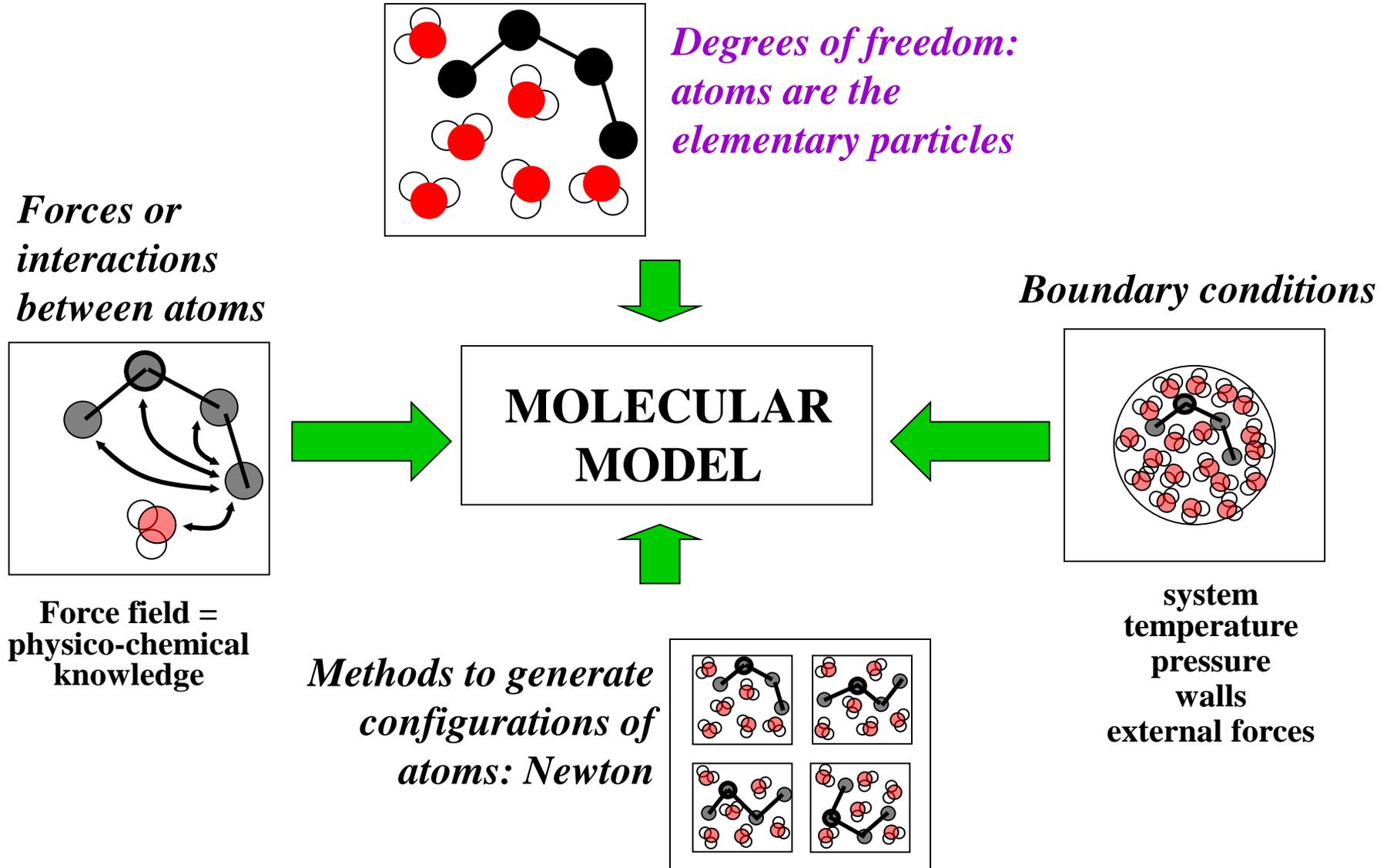
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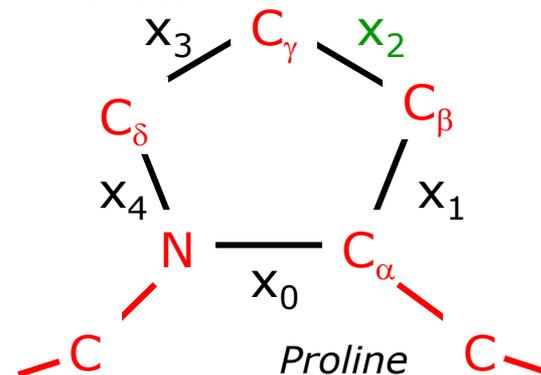
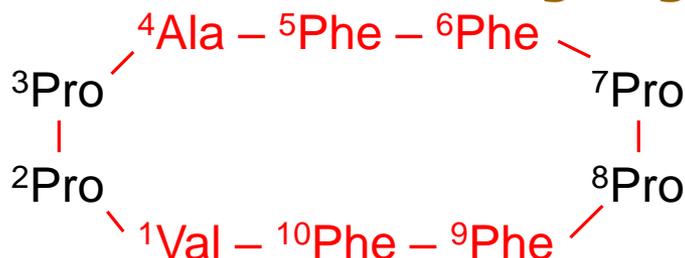
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# Definition of a model for molecular simulation



# Conformational Dynamics of Proline Residues in Antamanide: Effect of explicit solvent versus continuum: missing degrees of freedom



**Experiment : NMR** [<sup>13</sup>C relaxation  
E COSY] *R.R. Ernst*

3/8 Pro: rigid

2/7 Pro: 2 conformers (time constant ~ 30ps)

**Simulation: stochastic dynamics (500ps) SD**

## Comparison of <sup>3</sup>J<sub>HH</sub> coupling constants (in Hz) from NMR

Rms deviation simulation-experiment 1.5 Hz

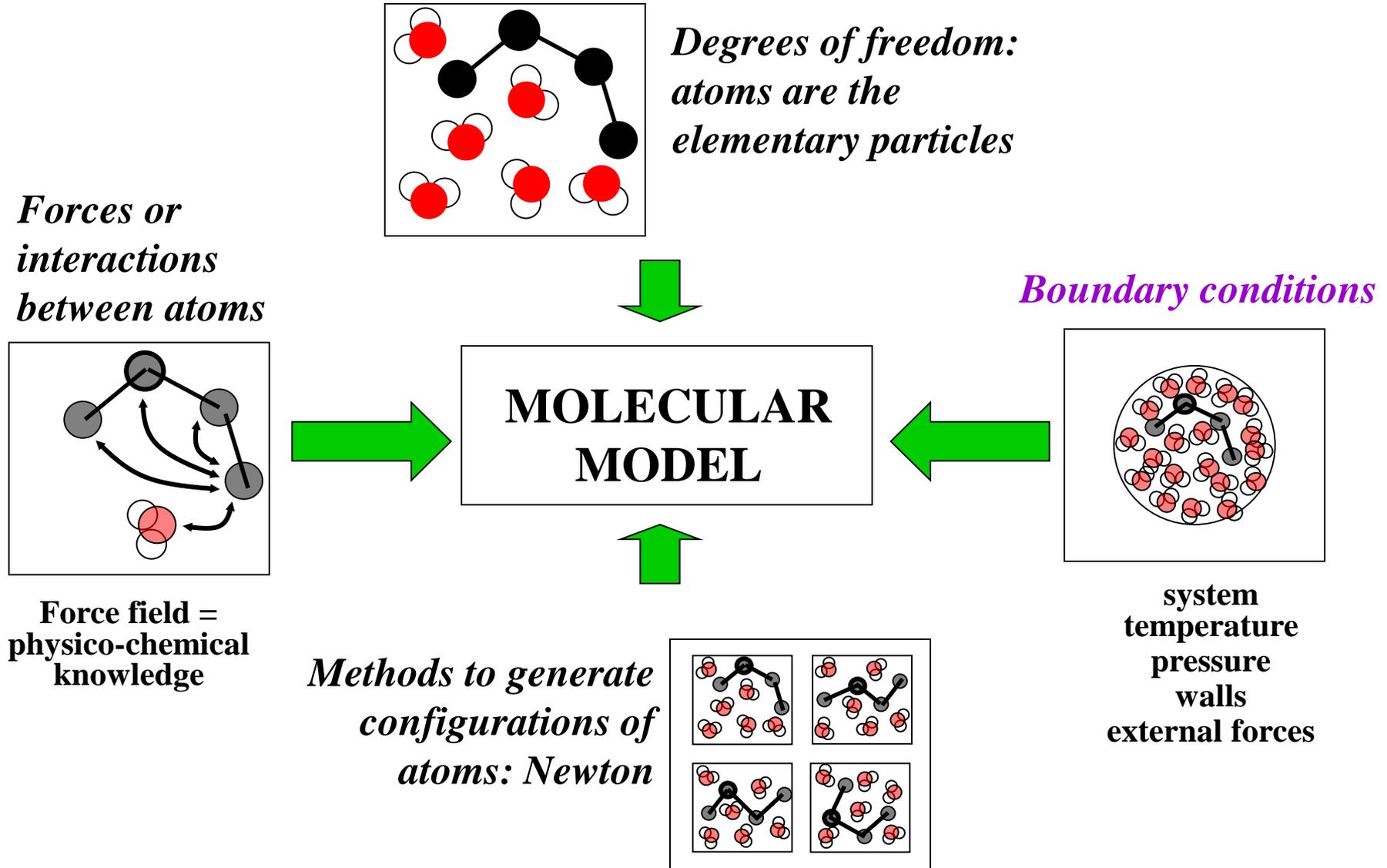
	Pro <sup>3</sup>		Pro <sup>8</sup>	
	NMR	SD	NMR	SD
$\alpha\beta_c$	8.5	7.9	8.1	8.0
$\alpha\beta_t$	1.1	2.3	0.9	2.4
$\beta_c\gamma_c$	6.8	8.7	6.8	8.7
$\beta_c\gamma_t$	12.0	9.8	13.0	9.7
$\beta_t\gamma_c$	2.4	2.2	1.4	2.3
$\beta_t\gamma_t$	6.5	8.6	6.4	8.5
$\gamma_c\delta_c$	7.6	8.7	7.3	8.6
$\gamma_c\delta_t$	2.1	3.4	1.5	3.4
$\gamma_t\delta_c$	10.3	7.6	10.9	7.7
$\gamma_t\delta_t$	8.5	8.9	8.8	8.8

Dynamics	GROMOS force field change	Friction coefficient $ps^{-1}$	Residence time $ps$
<b>Experiment</b>			<b>≈ 30</b>
<b>SD mean solvent</b>	-	<b>19</b>	<b>3</b>
<b>SD mean solvent</b>	-	<b>1000</b>	<b>25</b>
<b>SD mean solvent</b>	torsion x kT up	<b>19</b>	<b>25</b>
<b>MD explicit solvent</b>	-	-	<b>24</b>

*Solvent degrees of freedom are essential for dynamics*

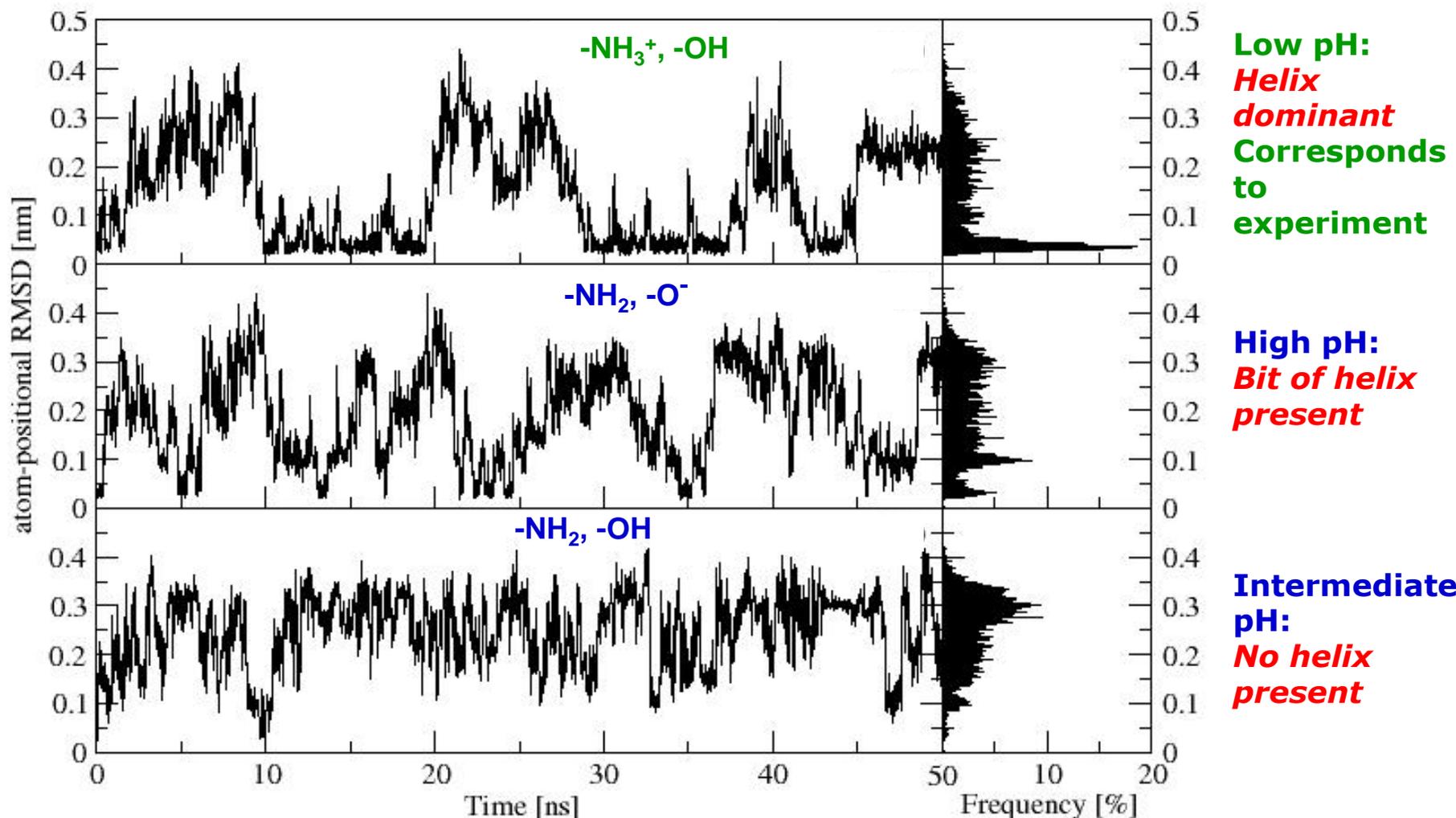
*R.M. Brunne et al., JACS, 115 (1993) 4764-4768  
J.W. Peng et al., J. Biomol. NMR 8 (1996) 453-476*

# Definition of a model for molecular simulation



# pH Dependence of the folding equilibrium of a $\beta$ -peptide in methanol solvent

## Backbone atom-positional RMSD from the helical fold



*Thermodynamic conditions chosen in a simulation may influence the result, i.e. the folding equilibrium*

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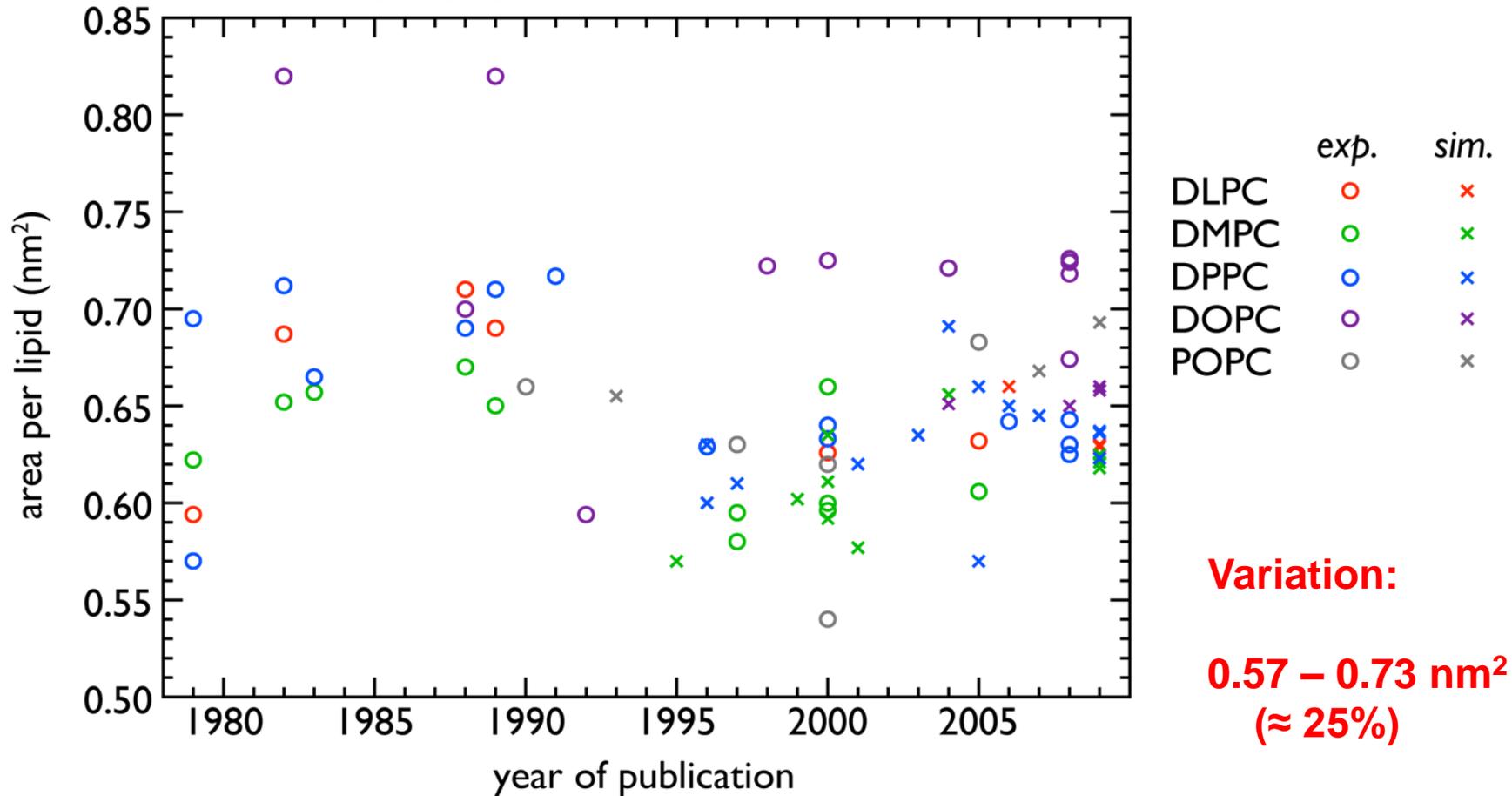
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# Modelling a specific membrane: area per lipid

*D. Poger & A.E. Mark, JCTC 6 (2010) 325-226*

## Area per lipid:

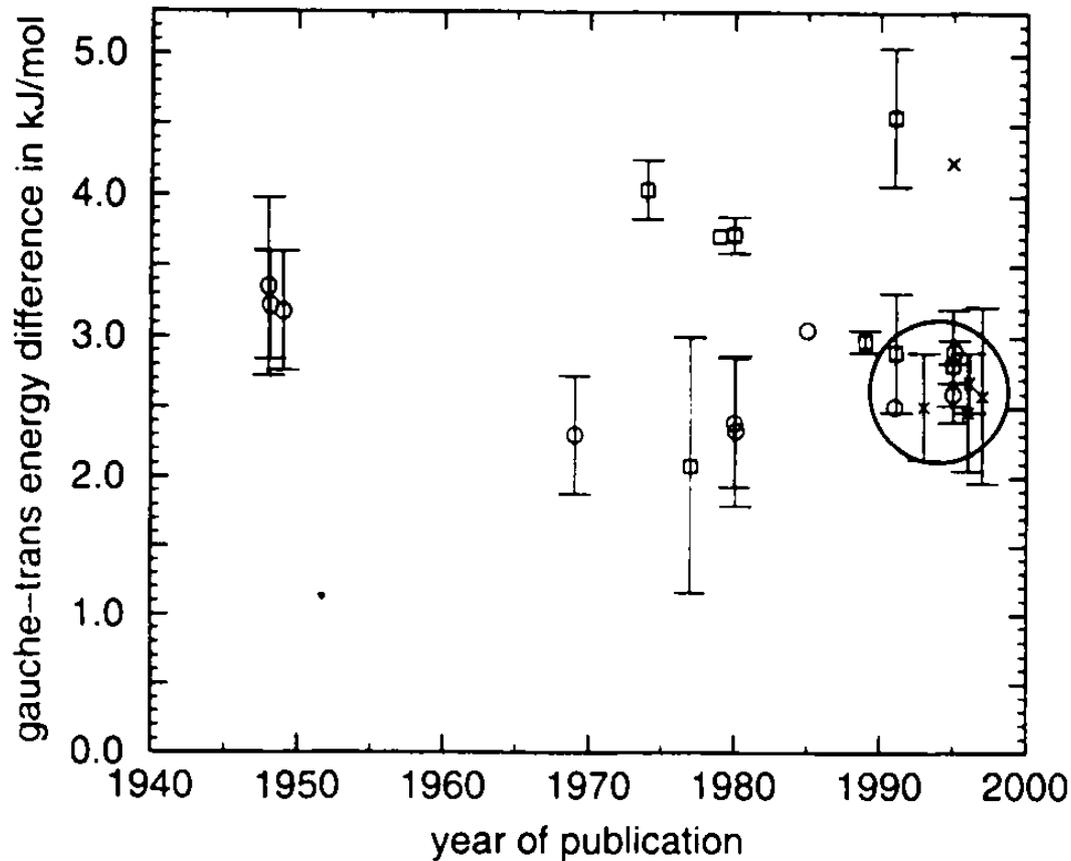
1. Most commonly used experimental quantity to validate a lipid model.
2. Difficult to measure directly.
3. Often inferred from NMR relaxation data.
4. Depends on measurement conditions.
5. Few research groups generate data.



**Experimental data vary with time**

# Variation over time in the experimental data regarding the trans-gauche energy difference in aliphatic chains

This quantity will influence the structure and mobility of lipid chains



Variation:  
2.0 to  
3.2 – 4.5 kJ/mol

Experimental data vary with time

# Test of Force Field and NMR Data for Hen Egg White Lysozyme

## Experimental Data

(Smith et. al., 1991, 1993; Buck et. al., 1995; Schwalbe et. al., 2001, both Oxford)

1158 NOE's derived inter-proton distances (set1 1993)

1525 NOE's derived inter-proton distances (set2 2001)

95  $^3J_{\text{HN}\alpha}$ -coupling constants

100  $^3J_{\alpha\beta}$ -coupling constants

124 backbone and 28 side-chain order parameters

X-ray coordinates (PDB 1aki, 1.5 Å)

NMR coordinates (PDB 1e8l, set of 50 structures)

Soares et al., *J. Biomol. NMR* 30 (2004) 407-422

van Gunsteren et al., *Angew. Chemie Intl. Ed.* 45 (2006) 4064-4092

# NOE distance bound violations in HEWL

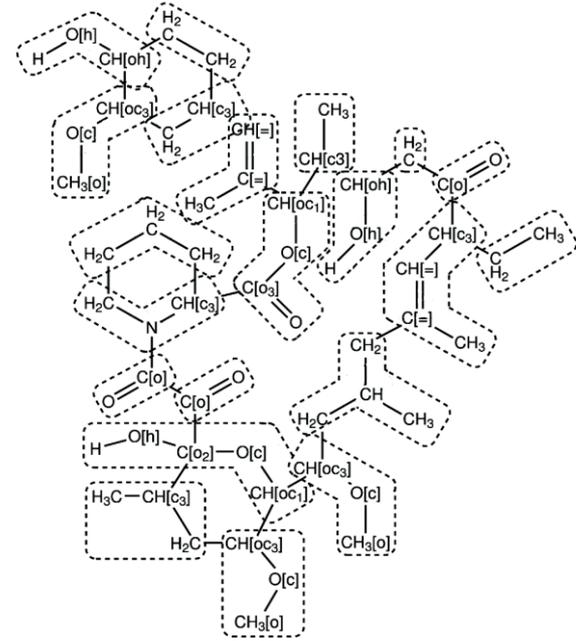
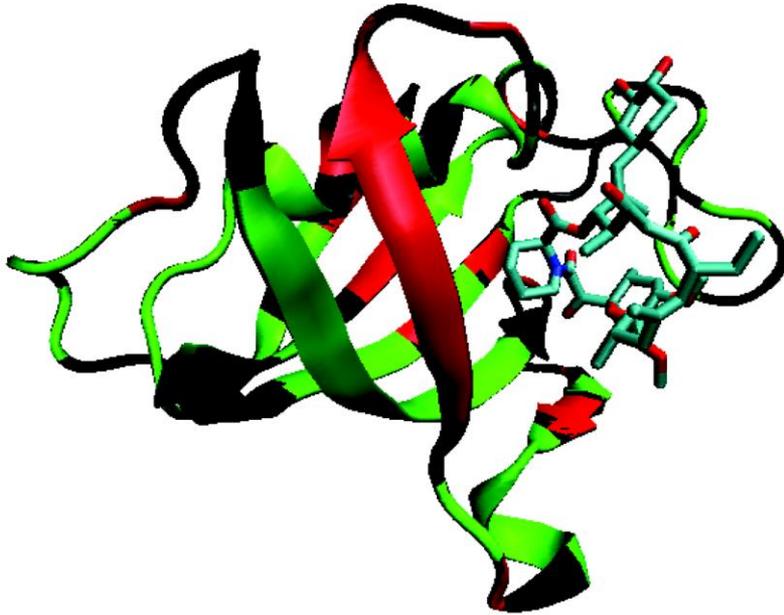
**NOE bound violations** computed from MD trajectories (43A1(1996)/45A3(2001)) against **two sets of experimental NOE distance bounds** from Smith *et. al.* (**set1, 1993**) and from Schwalbe *et. al.* (**set2, 2001**)

Averaging period (ns)	Number of violations (set1) <b>out of 1158 NOE's</b>			Mean violation <R <sub>E</sub> -R <sub>O</sub> >	
	>0.1 nm	>0.2 nm	> 0.3 nm		
	0.0-0.5	25/44	9/15		
0.5-1.5	31/44	11/15	3/3	0.020/0.024	<b>1993 set</b>
1.5-3.5	41/56	11/27	5/17	0.023/0.034	
0.0-3.5	23/43	9/17	3/6	0.019/0.026	
	Number of violations (set2) <b>out of 1525 NOE's (30% more)</b>				
	>0.1 nm	>0.2 nm	> 0.3 nm		
0.0-0.5	21/43	4/9	0/0	0.015/0.021	
0.5-1.5	22/47	2/14	0/2	0.017/0.021	<b>2001 set</b>
1.5-3.5	27/60	6/12	0/6	0.017/0.026	
0.0-3.5	20/40	2/7	0/1	0.014/0.020	

**Over time (1993 → 2001) the experimental data converged towards simulated ones**

# FKBP (107 residues) + ascomycin

## inconsistent experimental data



The protein is coloured according to whether or not there is a range of  $\chi_1$  dihedral angle values corresponding to the experimental  $^3J$ -coupling data ( $\pm 1$  Hz variation, distribution analysis):

black: no data (no  $^3J$ -couplings : 38; one  $^3J$ -coupling : 7 residues)

green: there is a single, continuous range of angle values that satisfies all of the experimental data (39 out of 62 residues: 63%)

red: there is no such solution (23 out of 62 residues: 37 %): **inconsistent ?**  
**yes, for 5 residues**

103  $^3J_{N-H\beta}$  and 94  $^3J_{H\alpha-H\beta}$ -values

# Interpretation of Experimental Data using Simulation

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**D4** Related but different quantities are compared, e.g. differently defined free energies of folding

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# Reasons for disagreement between $\langle Q \rangle_{sim}$ and $\langle Q \rangle_{exp}$

Related but different quantities are compared

$$\langle Q \rangle_{sim} \Leftrightarrow \langle Q' \rangle_{exp}$$

## 1. $Q'(\vec{r})$ is a **free energy change**

$$\Delta G_{\text{folding}} = G_{\text{fold}} - G_{\text{denatured}}$$

**of folding** or renaturation,

*as derived from experiment* by **changing the thermodynamic conditions**:

- *temperature change* ← Different solute stabilities
- pH change ← or
- ionic strength or *co-solvent change* ← free energies of folding  $Q'(\vec{r})$

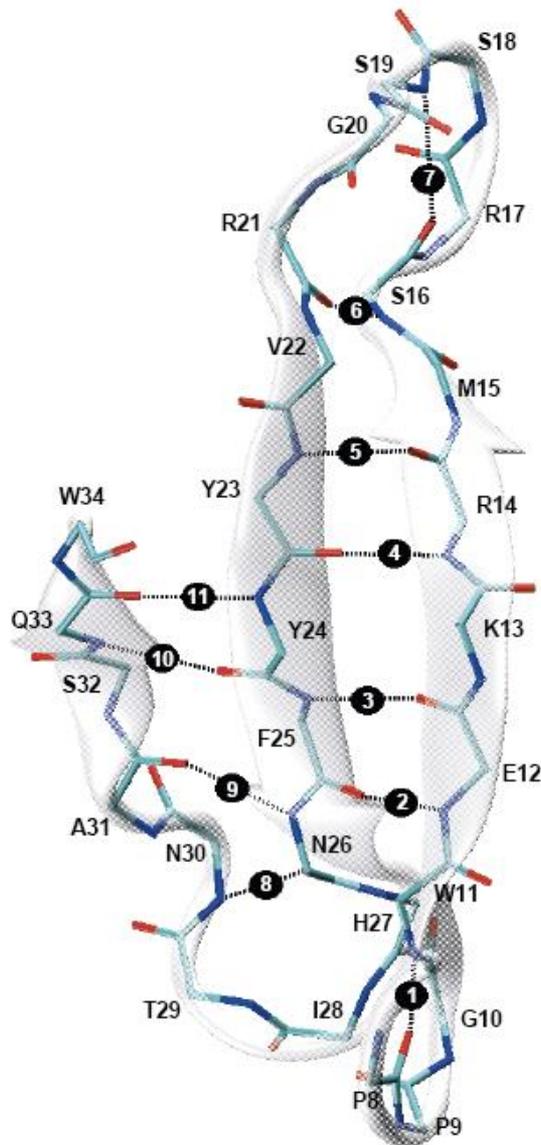
## 2. $Q(\vec{r})$ is a **free energy change**

$$\Delta G_{\text{folding}} = G_{\text{fold}} - G_{\text{unfolded}}$$

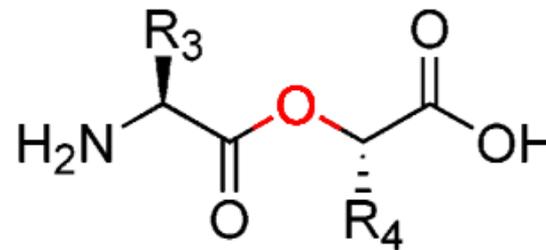
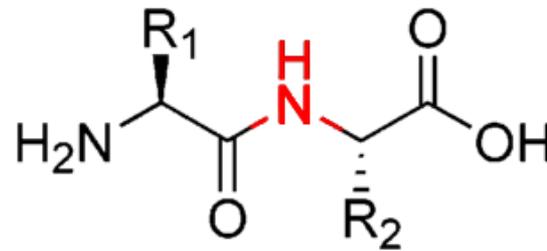
**of folding** *as derived from one simulation* at **one** given thermodynamic state point by **counting the ratio of folded versus unfolded conformations**

**Comparison has only limited value:  $\Delta G_{\text{folding}}(Q') \neq \Delta G_{\text{folding}}(Q)$**

# The WW domain of the PIN1 protein: Contribution of backbone hydrogen bonding to $\beta$ -sheet stability



11 backbone-backbone hydrogen bonds, distributed over three  $\beta$ -strands, each NH individually replaced by Oxygen



*Deechongkit et al.,  
JACS 126 (2004) 16762*

20 single residue mutants synthesised and their stability measured by experiments:

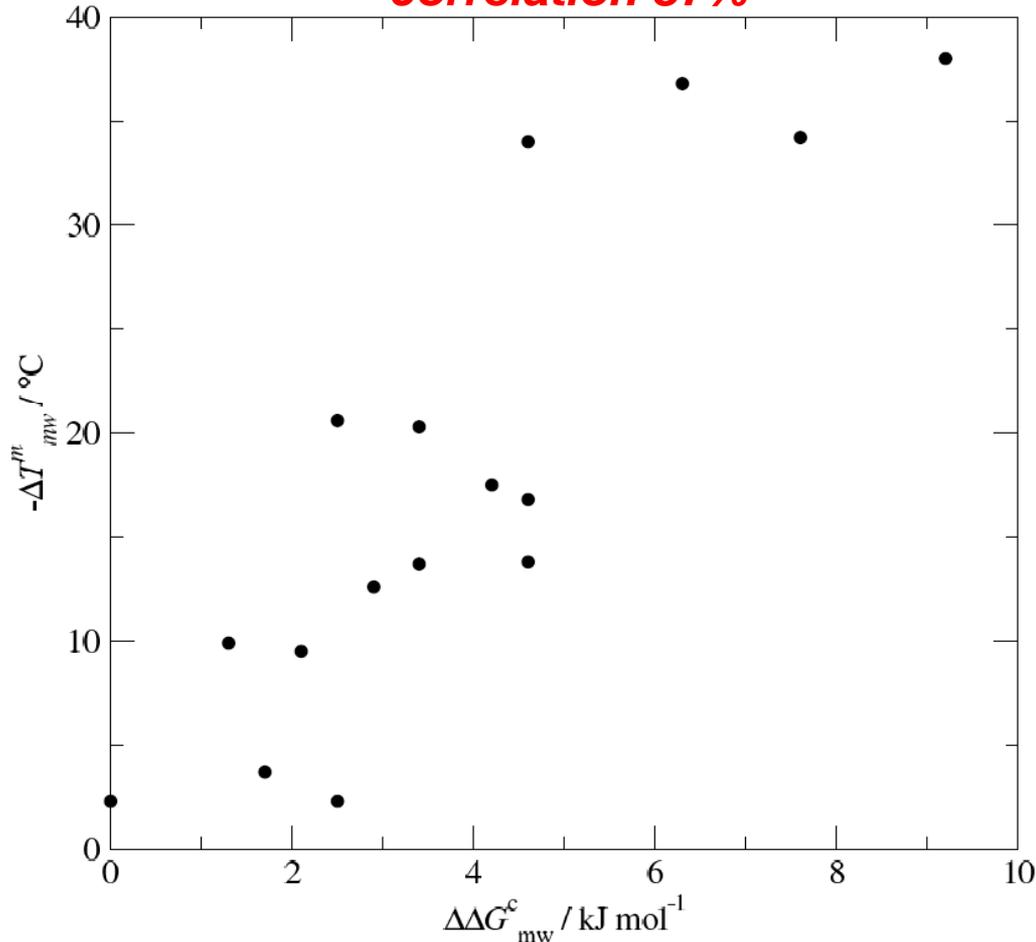
1. Thermal denaturation
2. Chaotrope denaturation (Gd-Cl)

# The WW domain of the PIN1 protein: Contribution of backbone hydrogen bonding to $\beta$ -sheet stability

Deechongkit et al.,  
JACS 126 (2004) 16762

Temperature versus chaotrope denaturation

**correlation 87%**



Dominant fold or structure  
of the 16 mutants verified by:

1. far-UV CD spectroscopy
2. fluorescence spectroscopy
3. 1D  $^1\text{H}$  NMR spectroscopy
4. ligand-binding assay

*R14 $\rho$ , F25 $\phi$ , N26 $\nu$ , Q33 $\theta$*   
*only stable upon addition of*  
*TMAO (trimethylamine N-oxide),*  
*no melting temperature*  
*reported*

**Different quantities reflecting fold stability need not show high correlation**

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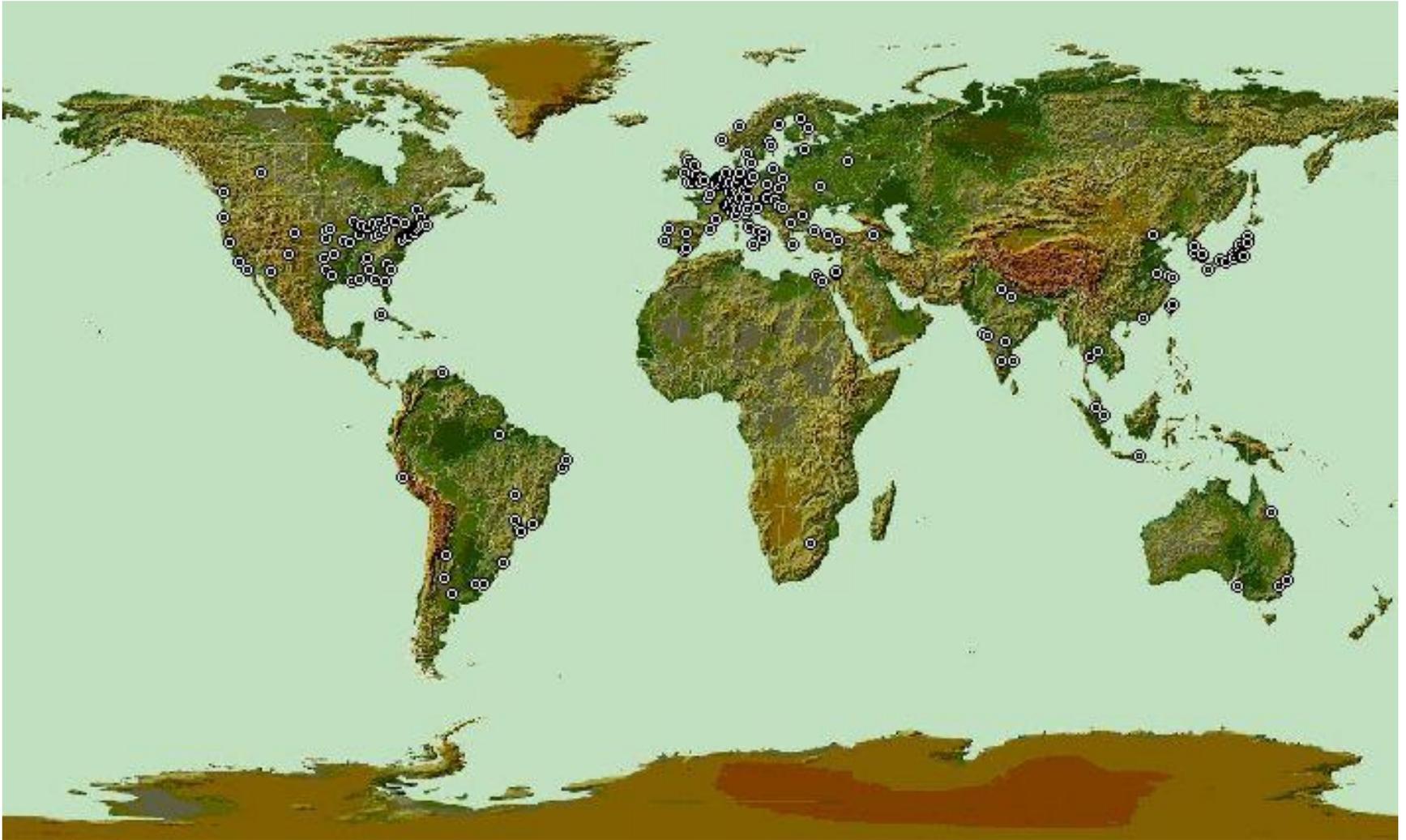
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# Spatial distribution of licences GROMOS biomolecular simulation software



**GROMOS = Groningen Molecular Simulation + GROMOS Force Field**

Generally available: <http://www.gromos.net>